## A circuit with four resistors



The equivalent resistance of the triplet  $R_2$ ,  $R_4$ , and  $R_3$  is  $R_T$  where

$$\frac{1}{R_T} = \frac{1}{R_2} + \frac{1}{R_4} + \frac{1}{R_3} = \frac{R_3R_4 + R_2R_3 + R_2R_4}{R_2R_4R_3},$$

and the equivalent resistance of the entire network is

$$R_{\rm eq} = R_1 + R_T = R_1 + \frac{R_2 R_4 R_3}{R_3 R_4 + R_2 R_3 + R_2 R_4}$$

Plugging in the numbers supplied,  $R_{\rm eq} = 1.5~\Omega + 1.5~\Omega = 3.0~\Omega.$ 



The fully reduced equivalent circuit above has

$$i = \frac{\mathcal{E}}{R_{\rm eq}} = \frac{6.0 V}{3.0 \Omega} = 2.0 \text{ A}.$$



Undoing the last equivalencing gives

$$i_1 = 2.0 \text{ A}$$
  $\Delta V_1 = i_1 R_1 = (2.0 \text{ A})(1.5 \Omega) = 3.0 \text{ V}$   
 $i_T = 2.0 \text{ A}$   $\Delta V_T = i_T R_T = (2.0 \text{ A})(1.5 \Omega) = 3.0 \text{ V}.$ 



Undoing the first equivalencing gives

$$i_{2} = \frac{\Delta V_{T}}{R_{2}} = \frac{3.0 \text{ V}}{4.0 \Omega} = 0.75 \text{ A}$$

$$i_{3} = \frac{\Delta V_{T}}{R_{3}} = \frac{3.0 \text{ V}}{4.0 \Omega} = 0.75 \text{ A}$$

$$i_{4} = \frac{\Delta V_{T}}{R_{4}} = \frac{3.0 \text{ V}}{6.0 \Omega} = 0.50 \text{ A}$$

(As a check, you can verify that  $i_1 = i_2 + i_3 + i_4$ .)

*Grading:* Students are asked to "Find the equivalent resistance of this network and the current through each resistor." They earn two points for each of these five items.