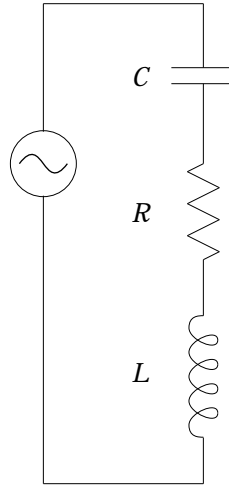


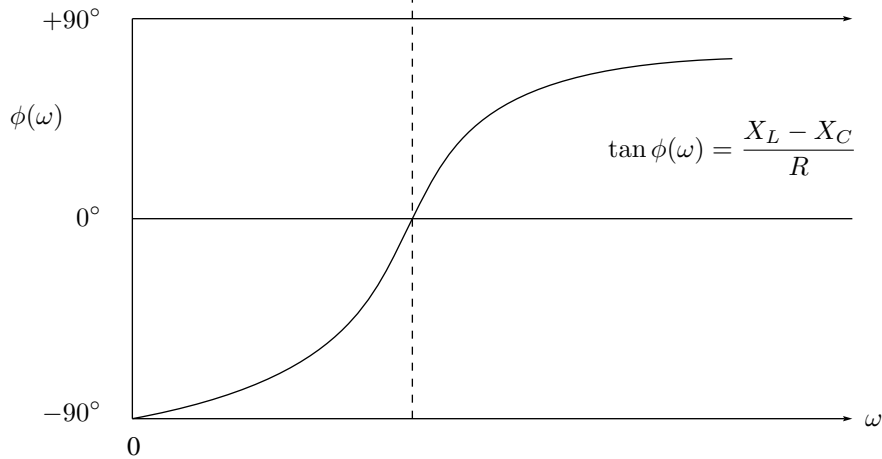
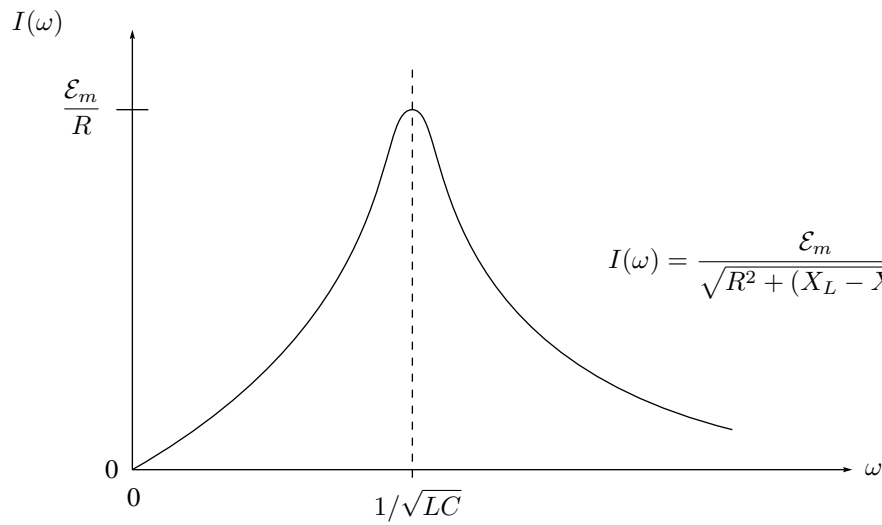
# The LCR circuit

$$\mathcal{E}(t) = \mathcal{E}_m \sin(\omega t)$$



$$i(t) = I(\omega) \sin(\omega t - \phi(\omega))$$

define reactance:  $X_C = \frac{1}{\omega C}$ ;  $X_L = \omega L$



**Slow changes** ( $\omega \ll 1/\sqrt{LC}$ )

- capacitive reactance dominates  $\Rightarrow I(\omega)$  small
- $v_C(t) \approx \mathcal{E}(t)$
- $\frac{q(t)}{C} \approx \mathcal{E}_m \sin(\omega t)$
- $i(t) = \frac{dq(t)}{dt} \approx C\mathcal{E}_m\omega \cos(\omega t)$
- c.f.  $i(t) = I \sin(\omega t - \phi) \Rightarrow \phi \approx -90^\circ$

**Fast changes** ( $\omega \gg 1/\sqrt{LC}$ )

- inductive reactance dominates  $\Rightarrow I(\omega)$  small
- $v_L(t) \approx \mathcal{E}(t)$
- $L \frac{di(t)}{dt} \approx \mathcal{E}_m \sin(\omega t)$
- $i(t) = \int \frac{di(t)}{dt} dt \approx -\frac{\mathcal{E}_m}{\omega L} \cos(\omega t)$
- c.f.  $i(t) = I \sin(\omega t - \phi) \Rightarrow \phi \approx +90^\circ$

**At resonance** ( $\omega = 1/\sqrt{LC}$ )

- $v_C(t)$  and  $v_L(t)$  can both be quite large, but
- $v_C(t) = -v_L(t)$  so  $v_R(t) = \mathcal{E}(t)$
- $\Rightarrow I(\omega) = \mathcal{E}_m/R$  (a maximum)
- $\phi(\omega) = 0^\circ$